## CEE 3804 Assignment 10 Solution

## Problem 1

## Task 1

The Simulink model to solve the non-linear ODE is shown below.


The sine wave block is used to generate the term: $\sin (\mathrm{t} / 2)$. Frequency 0.2 is equivalent to $\mathrm{t} / 2$.

| Parameters |  |  |
| :---: | :---: | :---: |
| Sine type: | Time based | * |
| Time ( t : | Use simulation time | $\hat{*}$ |
| Amplitude: |  |  |
| 1 : |  |  |
| Bias: |  |  |
|  |  |  |
| Frequency ( $\mathrm{rad} / \mathrm{sec}$ ): |  |  |
| 0.5 |  |  |
| Phase (rad): |  |  |
| 0 |  | ! |

## Task 2

Use initial conditions and parameters: $\mathrm{Ta}=15$ (C), $\mathrm{H}=0.08$ ( $1 /$ minute), $\mathrm{T}_{0}=150$ (C)

Task 3


```
%% Problem 1 Task 3
Time_mins=out.ScopeData(:,1);
Temp_asphalt_degree_C=out.ScopeData(:,2);
h1=plot(Time_mins,Temp_asphalt_degree_C);
grid on
h1.Color='b';
h1.LineWidth=1.5;
xlabel('Time (mins)',FontSize=15)
ylabel('Asphalt Temperature (degrees C.)',FontSize=15)
```

Task 4
The first time within $3 \%$ is 68.4 minutes.

```
%% %% Problem 1 Task 4
idx=find(Temp_asphalt_degree_C<=15*1.03);
the_first_time_within_3percent=Time_mins(idx(1));
disp(['The first time within 3% is ',num2str(the_first_time_within_3percent),' minutes.'])
```


## Problem 2

## Task 1

## Method 1 (learned in class)

Function (below) to estimate the rate of change of temperature $(T)$ with time $(t)$.

```
% First Order Differential Equation Function
% where:
% H is a cooling constant (1/time)
% T is the temperature of the element of interest (deg C)
% Ta is the ambient temperature (deg C)
function [tprime] = ftem(t,T)
global Ta H
% tprime = - H * (T - Ta);
tprime = - H * (T-Ta) - sin(t/2)* (T-Ta)/12;
tprime = tprime';
```

Matlab script (below) to call the function above and solve the problem using ODE45 solver.

```
% Solution to First-Order Equation of the form:
%
% dT/dt = - H * (T - Ta)
%
% subject to initial conditions:
%
% T (t=0) = To
%
% where:
% H is a cooling constant (1/time)
% T is the temperature of the element of interest (deg C)
% Ta is the ambient temperature (deg C)
global Ta H
% Define Initial Conditions of the Problem
To =150; % To is the initial temperature of the fin
to =0.0; % to is the initial time to solve this equation (min)
tf=90; % tf is the final time (min)
% define T ambient (Ta) and cooling constant (H)
Ta=15;
H = 0.08;
tspan =[to tf];
[t,T] = ode45('ftem',tspan,To);
```



Temperature profile using ODE45.

## Method 2 with embedded function into Matlab script

```
function dydt = myode(t,y,ft,f,gt,g)
f = interp1(ft,f,t); % Interpolate the data set (ft,f) at time t
g = interp1(gt,g,t); % Interpolate the data set (gt,g) at time t
dydt = -f.*y + g; % Evaluate ODE at time t
end
%% Problem 2 Task 1
ft = linspace(0,90,901);
f = 0.08+sin(ft*0.5)*1/12;
gt = linspace(0,90,901);
g = 15*0.08+sin(gt*0.5)*15/12;
tspan = [0 90];
ic = 150;
%opts = odeset('RelTol',1e-2,'AbsTol',1e-4);
[Time_mins_p2,Temp_asphalt_degree_C_p2] = ode45(@(t,y) myode(t,y,ft,f,gt,g), tspan, ic);
```

Task 2
According to the following two lines, we can find that the solution is the same.

\%\% Problem 2 Task 2
subplot(2,1,1)
h1=plot(Time_mins,Temp_asphalt_degree_C);
grid on
h1.Color='b';
h1.LineWidth=1.5;
h1.Marker='o';
xlabel('Time from Simulink Result (mins)',FontSize=14)
ylabel('Asphalt Temperature (degrees C)',FontSize=14)
subplot(2,1,2)
h2=plot(Time_mins_p2,Temp_asphalt_degree_C_p2);
grid on
h2. Color='r';
h2. LineWidth=1.5;
h2.Marker='o';
xlabel('Time from ODE45 Result (mins)',FontSize=14)
ylabel('Asphalt Temperature (degrees C)', FontSize=14)

